

National University

**Faculty of Engineering and
Architecture**

Ohm's Law

Ohm's Law

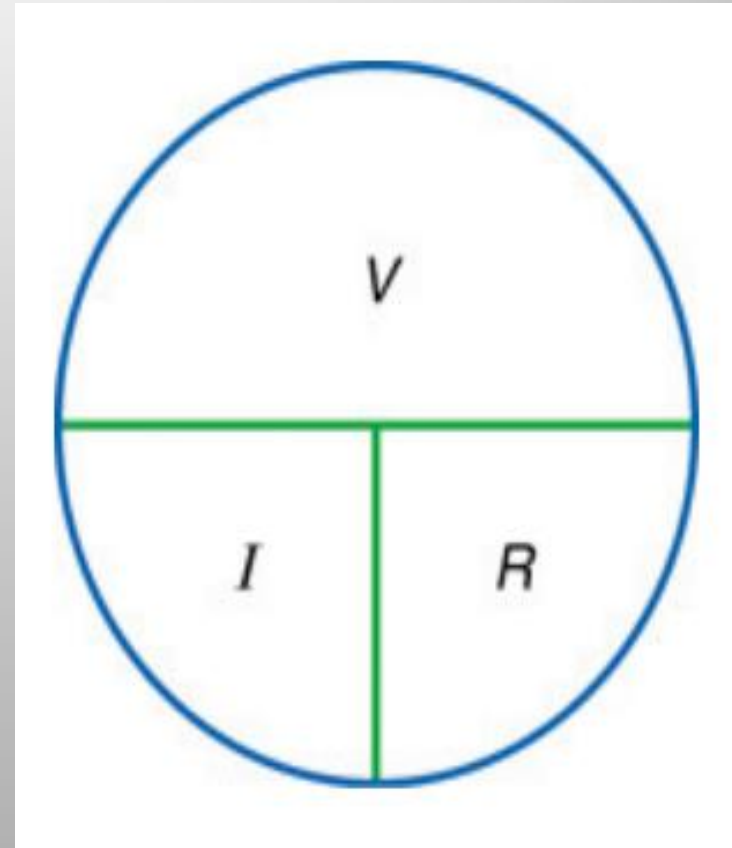
- The most fundamental law in electricity is Ohm's law.
- Ohm's law states that, in an electrical circuit, the current passing through most materials is directly proportional to the potential difference applied across them.

There are three forms of Ohm's Law:

$$I = V/R \quad V = IR \quad R = V/I$$

where:

- V is for voltage which is measurement of the work required to move a unit charge between two points.
- I is current which is the measurement of the flow of charge in a circuit.
- R is resistance which resists current flow



Multiple and Submultiple Units

Units of Voltage:

- The basic unit of voltage is the volt (V).
- Multiple units of voltage are: 1- kilovolt (kV) or 10^3 V
2- megavolt (MV) or 10^6 V
- Submultiple units of voltage are:
1- millivolt (mV) or 10^{-3} V
2- microvolt (μ V) or 10^{-6} V

Units of Current

- The basic unit of current is the ampere (A).
- Submultiple units of current are:
1- milliampere (mA) or 10^{-3} A
2- microampere (μ A) or 10^{-6} A

Continued: Units of Resistance

- The basic unit of resistance is the Ohm (Ω).
Multiple units of resistance are:

1- kilo ohm ($k\Omega$) 1 thousand ohms or $10^3 \Omega$

2- Mega ohm ($M\Omega$) 1 million ohms or $10^6 \Omega$

Examples:

- How much is the current, I , in a $470\text{-k}\Omega$ resistor if its voltage is 23.5 V ?
- How much voltage will be dropped across a $40\text{ k}\Omega$ resistance whose current is $250\text{ }\mu\text{A}$?
- How much resistant will be added to electrical circuit when current through it $I = 2\text{ mA}$ and its voltage $V=14\text{V}$?

The Linear Proportion between V and I:

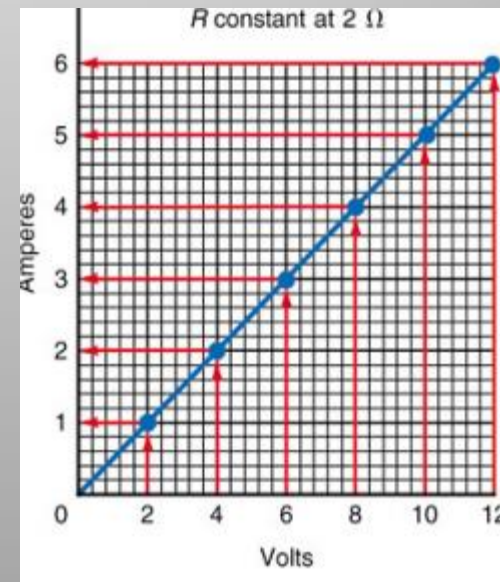
1- When R is constant:

- I increases as V increases
- I decreases as V decreases

2- When V is constant:

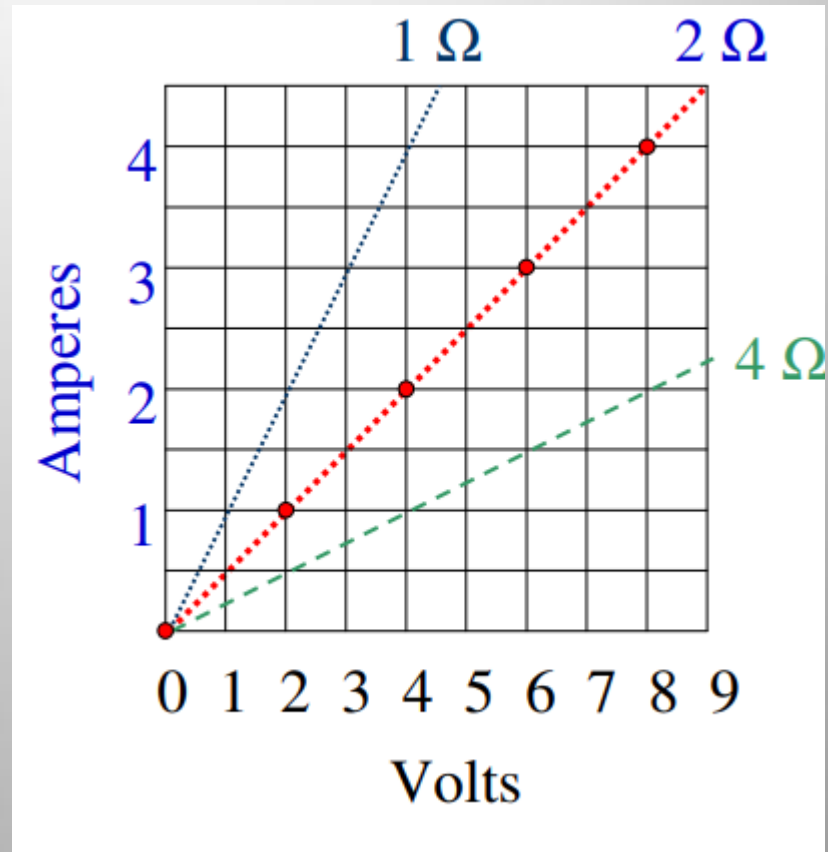
- I decreases as R increases.
- I increases as R decreases.
- Examples:
 - If R doubles, I is reduced by half.
 - If R is reduced to $\frac{1}{4}$, I increases by 4.

Volts V	Ohms Ω	Amperes A
0	2	0
2	2	1
4	2	2
6	2	3
8	2	4
10	2	5
12	2	6



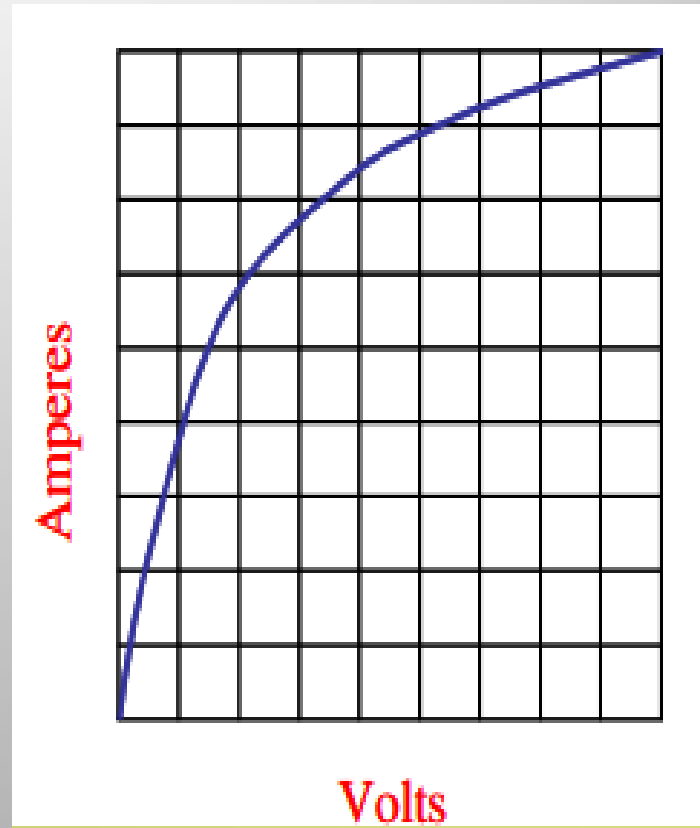
Linear Resistance:

- has a constant value of ohms.
- Its R does not change with the applied voltage, so V and I are directly proportional.
- Carbon-film and metal-film resistors are examples of linear resistors.



Nonlinear Resistance

- In a nonlinear resistance, increasing the applied V produces more current, but I does not increase in the same proportion as the increase in V .
- Example of V and I non-linear relationship:
- As the tungsten filament in a light bulb gets hot, its resistance increases.



Power:

- It is the time rate of doing work. It equals the product of voltage and current.

$$P = V \times I$$

- The basic unit of power is the watt (W).
- Multiple units of power are:
 - kilowatt (kW): 10^3 W
 - megawatt (MW): 10^6 W
- Submultiple units of power are:
 - Milli watt (mW): 10^{-3} W
 - microwatt (μ W): 10^{-6} W

Kilowatt Hours:

- is a unit commonly used for large amounts of electrical work or energy.
- For example, electric bills.
- The amount of work (energy) can be found by multiplying power (in kilowatts) \times time in hours.

Cost:

- Can be found by multiplying (KWH) by assuming rate for the device.
- Example:

An air conditioner operates at 240 volts and 20 amperes.

The power is $P = V \times I = 240 \times 20 = 4800$ watts.

Convert to kilowatts: 4800 watts = 4.8 kilowatts

Continued:

- Multiply by hours: (Assume it runs half the day)
energy = $4.8 \text{ kW} \times 12 \text{ hours} = 57.6 \text{ kWh}$
- Multiply by rate: (Assume a rate of \$0.08/ kWh)
cost = $57.6 \times \$0.08 = \4.61 per day

Power Formulas:

- There are three basic power formulas, but each can be in three forms for nine combinations.
- All nine power formulas are based on Ohm's Law.

$$\mathbf{V = IR}$$

$$\mathbf{I = \frac{V}{R}}$$

$$\mathbf{P = VI}$$

Continued:

- Substitute IR for V to obtain:

$$P = VI = (IR)I = I^2R$$

- Substitute V/R for I to obtain:

$$P = VI = V \times V/R = V^2 / R$$

Continued:

$$P = VI$$

$$I = \frac{P}{V}$$

$$V = \frac{P}{I}$$

$$P = I^2R$$

$$R = \frac{P}{I^2}$$

$$I = \sqrt{\frac{P}{R}}$$

$$P = \frac{V^2}{R}$$

$$R = \frac{V^2}{P}$$

$$V = \sqrt{PR}$$

- Where: P = Power V = Voltage I = Current
R=Resistance

Examples:

- What is the resistance of a device that dissipates 1.2 kW of power when its current is 10 A?
- How much current does a 960 W coffeemaker draw from the 120 V power line?
- What is the resistance of a 20 W, 12 V halogen lamp?

Choosing a Resistor for a Circuit:

- Follow these steps when choosing a resistor for a circuit:

1- Determine the required resistance value as $R = V / I$.

2- Calculate the power dissipated by the resistor using any of the power formulas.

3- Select a wattage rating for the resistor that will provide an adequate cushion between the actual power dissipation and the resistor's power rating.

4- Ideally, the power dissipation in a resistor should never be more than 50% of its power rating.

Example:

- Determine the required resistance and appropriate wattage rating of a carbon-film resistor to meet the following requirements: The resistor has a 54-V drop when its current is 20 mA.

The resistors available have the following wattage ratings: $1/8$ W, $1/4$ W, $1/2$ W, 1 W, and 2 W.