

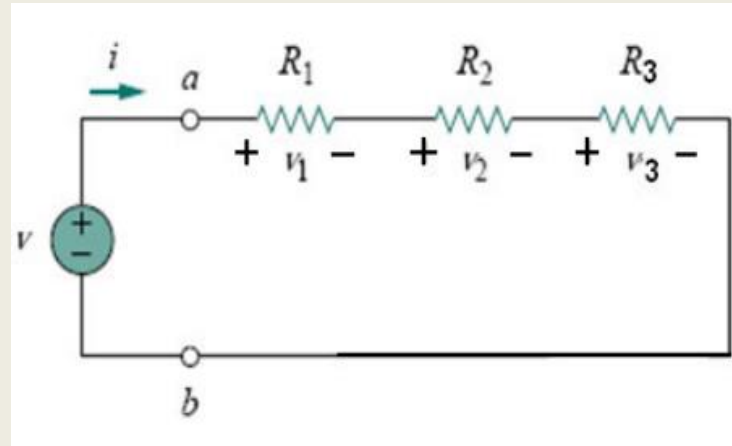
National University

**Faculty of Engineering and
Architecture**

Voltage and Current Division

1- Voltage Division:

- The source voltage v is divided among the resistors in direct proportion to their resistances
- The larger the resistance, the larger the voltage drop.

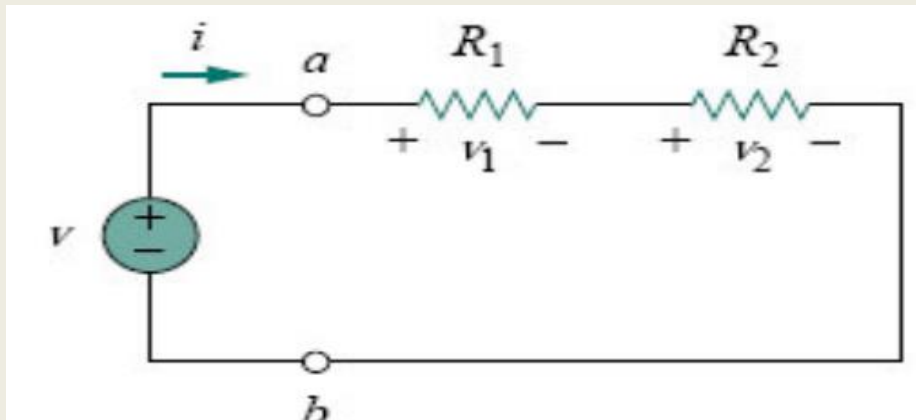


we know $i = V_{TOTAL} / (R_1 + R_2 + R_3)$
so the voltage over the first resistor is
 $V_1 = i R_1$ $V_1 = R_1 V_{TOTAL} / (R_1 + R_2 + R_3)$

$$v_1 = V \frac{R_1}{R_1 + R_2 + R_3}$$

Example:

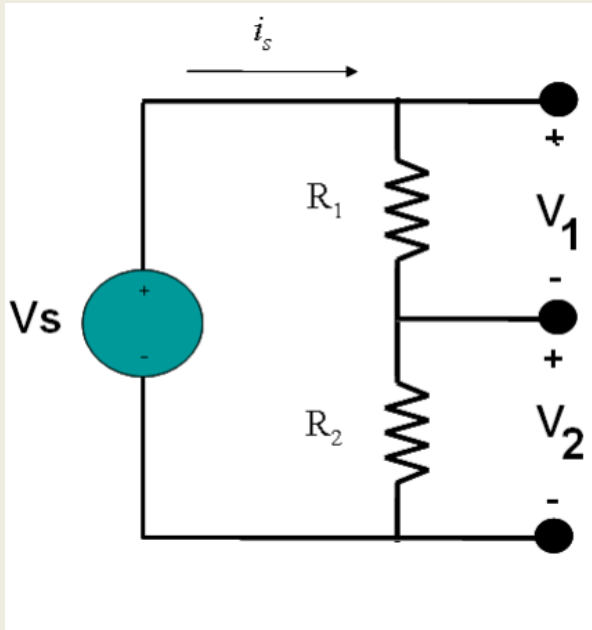
- determine the voltage across each resistor



$$v_1 = \frac{R_1}{R_1 + R_2} v$$
$$v_2 = \frac{R_2}{R_1 + R_2} v$$

Example:

- determine the voltage across each resistor

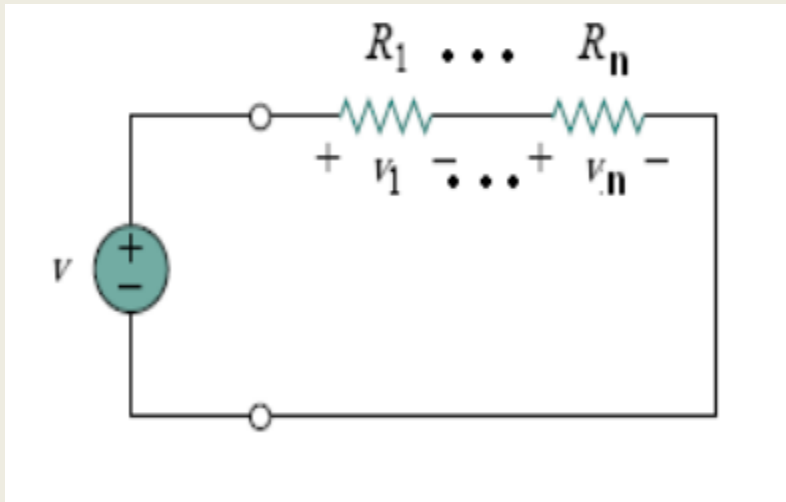


$$i_s = \frac{V_s}{R_1 + R_2}$$
$$v_1 = \frac{R_1}{R_1 + R_2} v_s$$
$$v_2 = \frac{R_2}{R_1 + R_2} v_s$$

The equations for v_1 and v_2 are annotated with red circles around the fraction and red arrows pointing to the i_s label, indicating that the voltage across each resistor is the current i_s multiplied by its resistance.

In general :

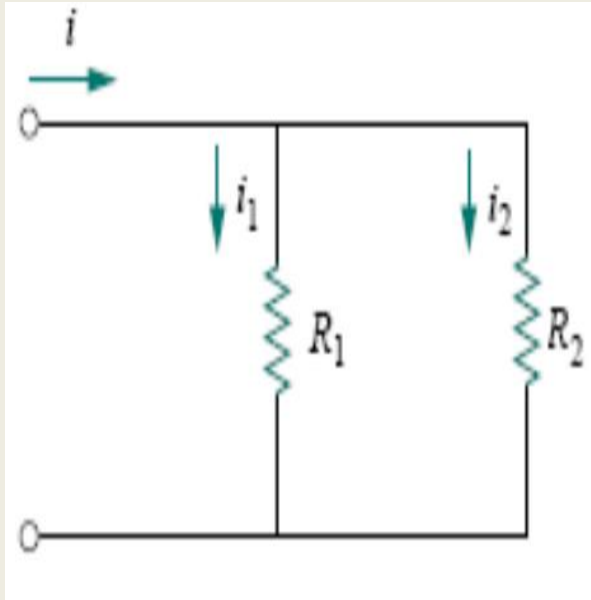
- If a voltage divider has N resistors (R_1, R_2, \dots, R_N) in series with the source voltage v , the n th resistor (R_n) will have a voltage drop of:



$$v_n = \frac{R_n}{R_1 + R_2 + \dots + R_N} v$$

2- Current Division:

- If we know the current flowing into two parallel resistors:



$$v = i \frac{R_1 R_2}{R_1 + R_2} \leftarrow R_{Eq}$$

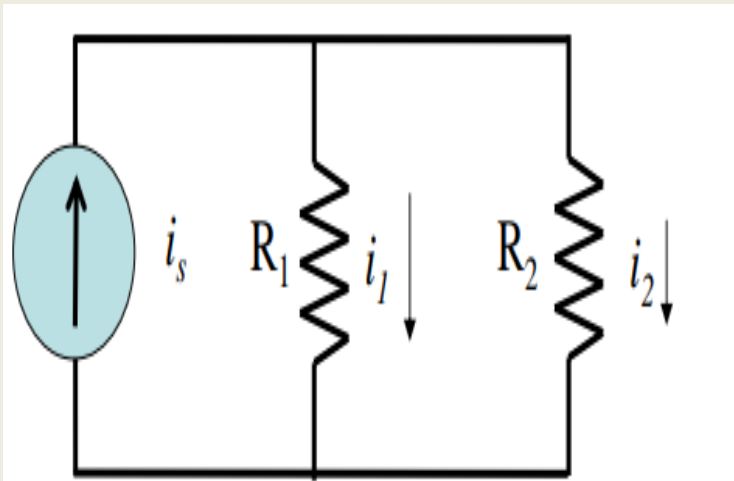
$$i_1 = \frac{v}{R_1}$$

$$i_1 = \frac{1}{R_1} \left[i \frac{R_1 R_2}{R_1 + R_2} \right]$$

$$i_1 = i \frac{R_2}{R_1 + R_2}$$

Example:

- Find i_1 and i_2 in terms of i_s



$$i_s = i_1 + i_2$$

$$v_1 = v_2$$

$$i_1 R_1 = i_2 R_2$$

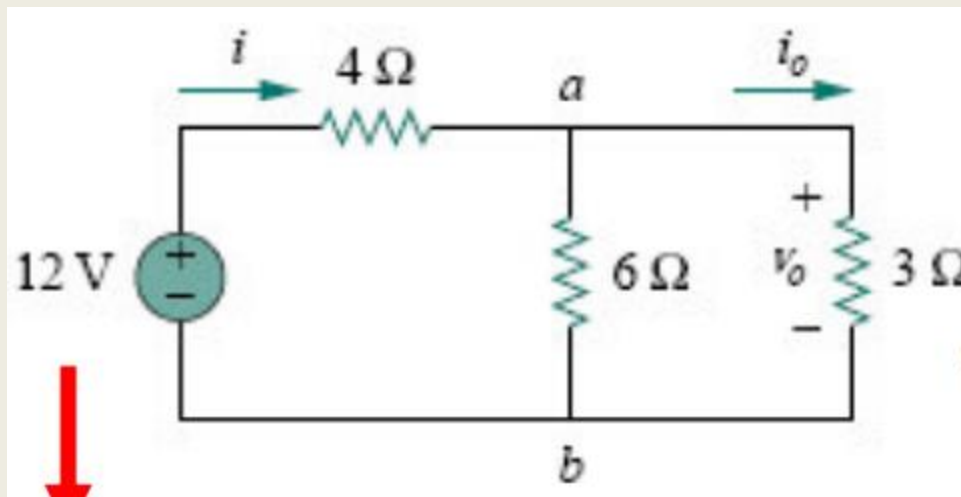
$$i_2 = i_1 \frac{R_1}{R_2} \Rightarrow i_s = i_1 + i_1 \frac{R_1}{R_2} = i_1 \left(\frac{R_2 + R_1}{R_2} \right)$$

$$i_1 = i_s \left(\frac{R_2}{R_1 + R_2} \right)$$

$$i_2 = i_s \left(\frac{R_1}{R_1 + R_2} \right)$$

Example:

- Use Voltage and current division rules to find V_o and i_o :



For more examples:

- <https://youtu.be/dil7O8vRsy0>